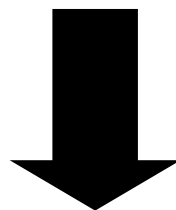


# Background

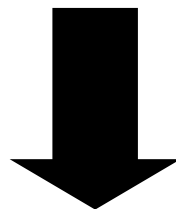
**Frequency is a fundamental physical quantity of electromagnetic wave**

*Maintenance of THz frequency metrology is required for various THz applications*



*Advent of practical CW-THz sources (THz-QCL, photomixing with UTC-PD, RTD etc)*

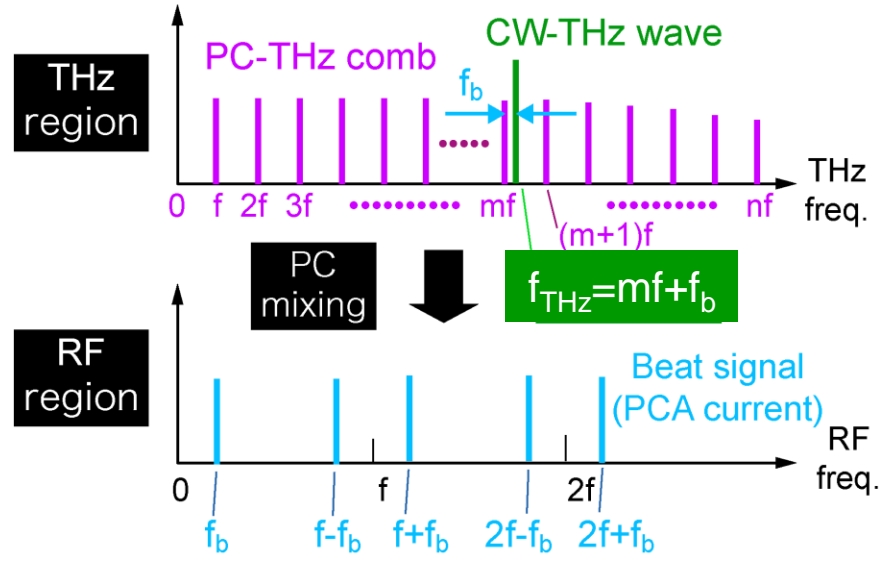
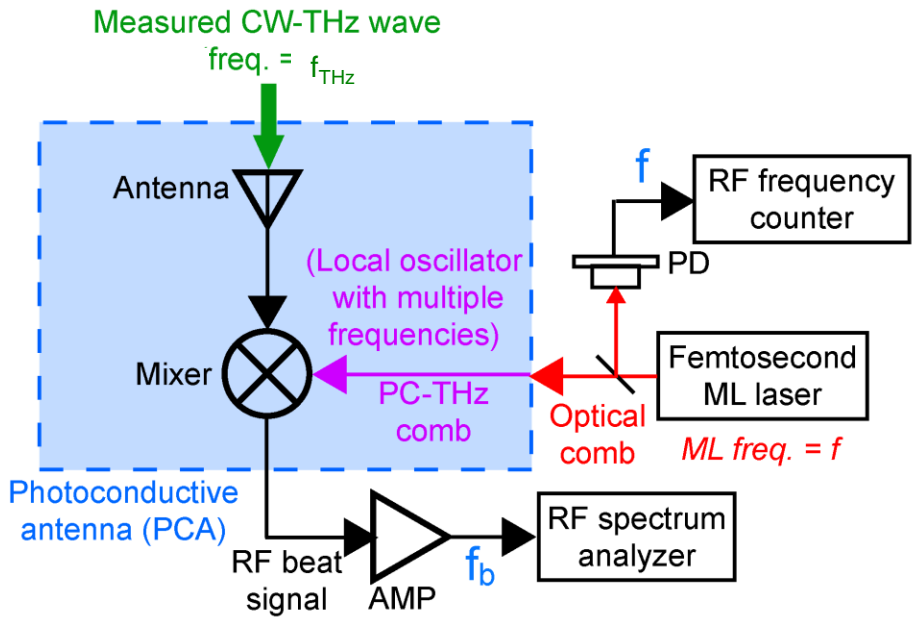
**Precise frequency measurement of CW-THz wave is required!**



**However, techniques of absolute frequency measurement of CW-THz wave are still immature!**

# THz spectrum analyzer (1)

## Freq. domain



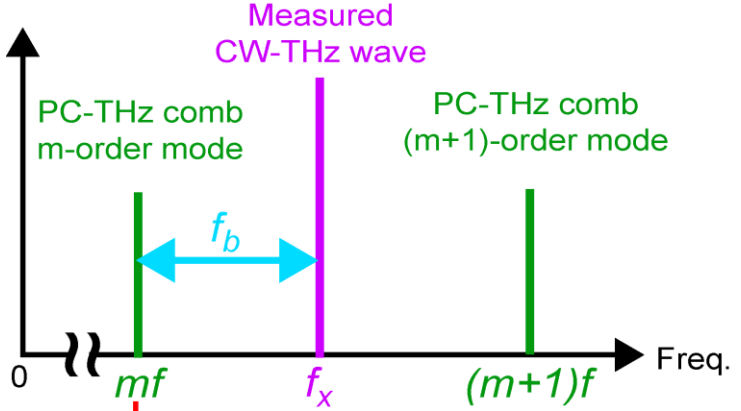
$$f_{\text{THz}} = mf \pm f_b$$

*m*: order of comb mode  
*f*: ML frequency  
*f<sub>b</sub>*: beat frequency

Ref) S. Yokoyama et al, *Opt. Express* **16**, 13052-13061 (2008).

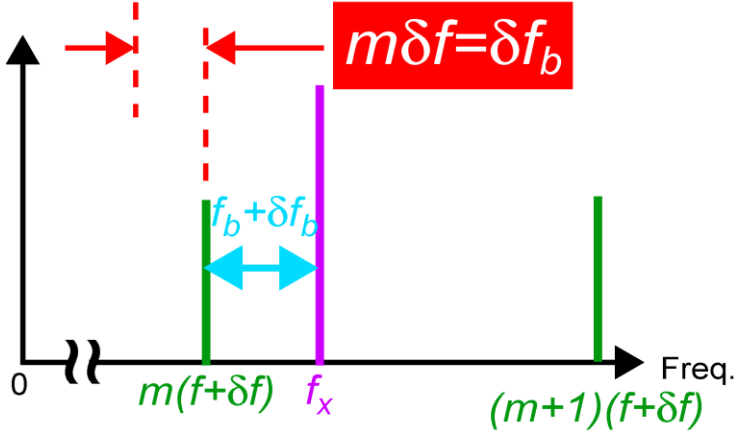
T. Yasui et al. *Opt. Express* **17**, 17034-17043 (2009).

# THz spectrum analyzer (2)



Shift of ML freq. by  $\delta f$   
 $(f \rightarrow f + \delta f)$

$$m = \frac{|\delta f_b|}{|\delta f|}$$



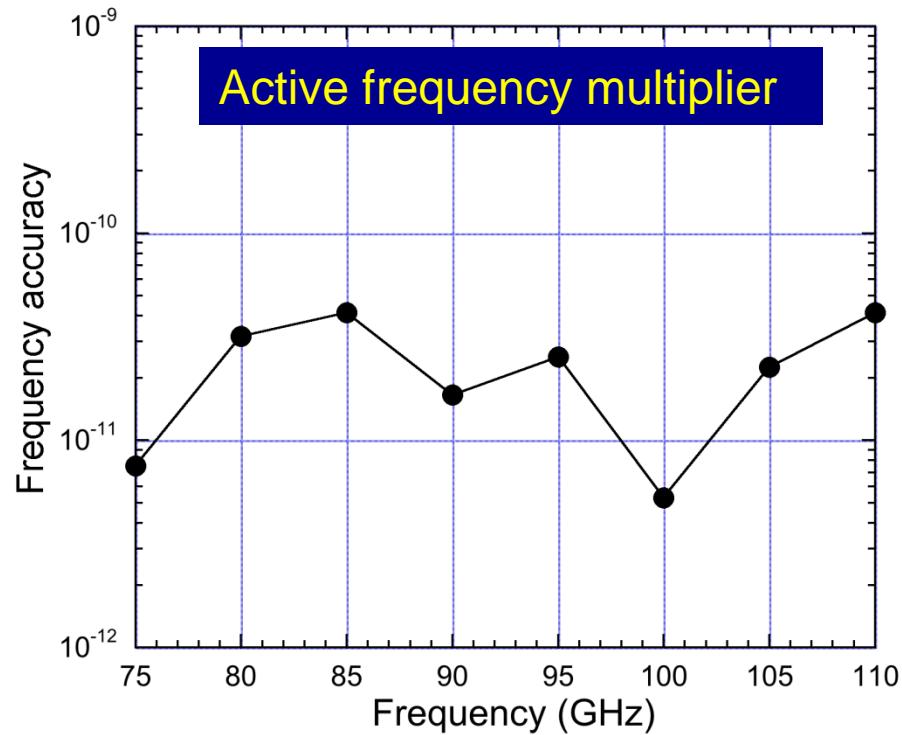
Change of beat freq. by  $\delta f_b$   
 $(f_b \rightarrow f_b + \delta f_b)$

$$f_{THz} = mf - f_b \quad (\delta f_b / \delta f > 0)$$

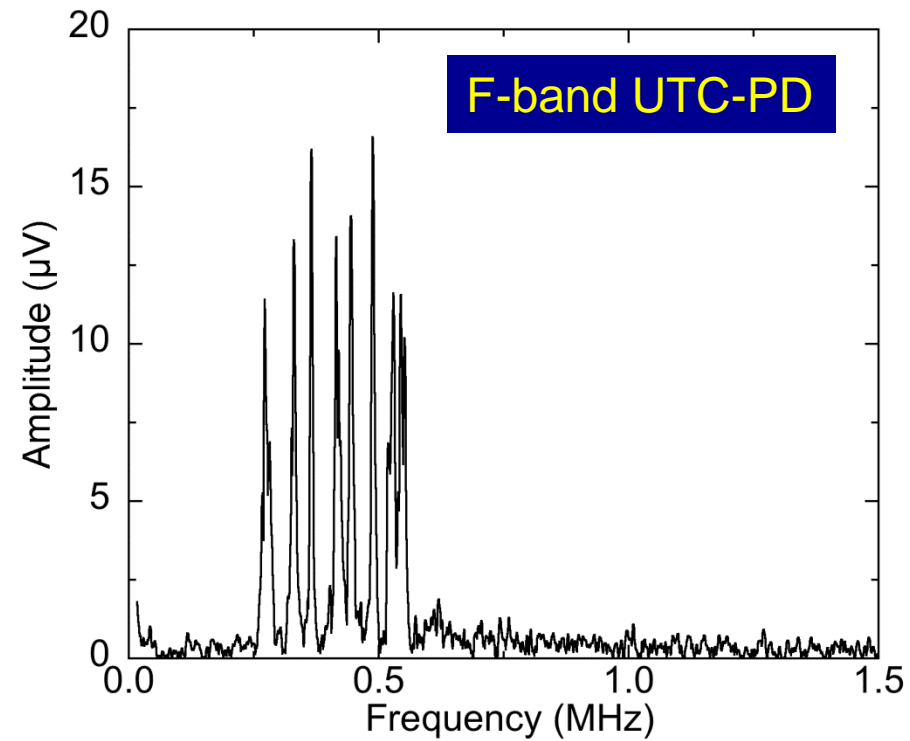
$$f_{THz} = mf + f_b \quad (\delta f_b / \delta f < 0)$$

# Previous study



## Absolute frequency measurement

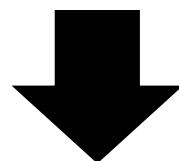


## Real-time monitoring of CW-THz wave



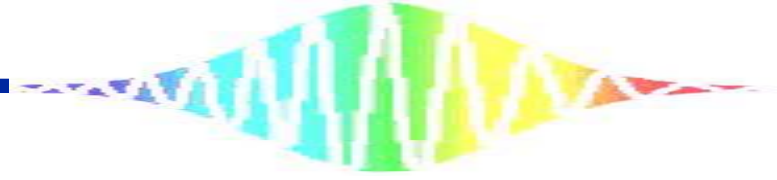
# Problems of previous studies for practical use

- (1) 2-step measurements of beat signal for absolute frequency determination  **Not real-time!**
- (2) Coupling of PCA with 1.5- $\mu\text{m}$  fiber laser light using free-space optics  **Not portable!**



## Present talk

- (1) **Real-time determination** of absolute frequency using dual PC-THz combs
- (2) **Direct coupling** of LT-GaAs-PCA with output fiber tip of 1.5 $\mu\text{m}$  fiber laser

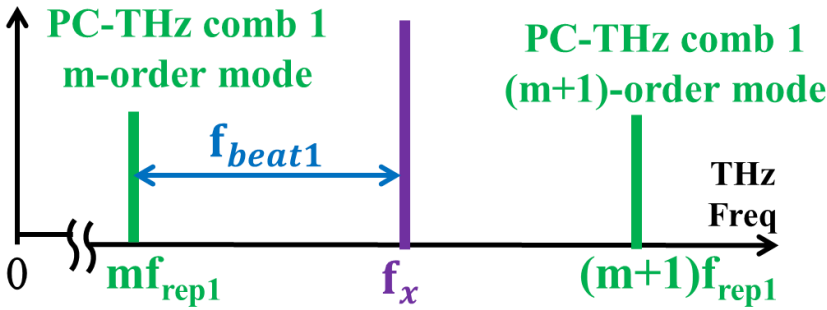


(1) Real-time determination of absolute frequency using dual PC-THz combs

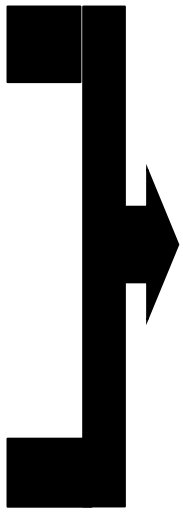
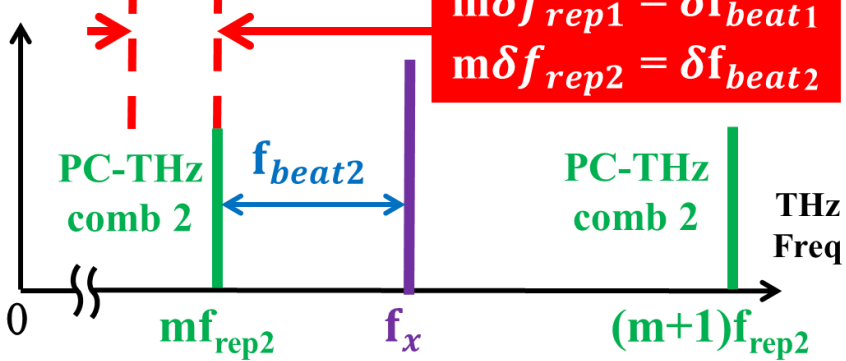


# Real-time determination of absolute frequency

Laser A  
(PC-THz comb 1)



Laser B  
(PC-THz comb 2)

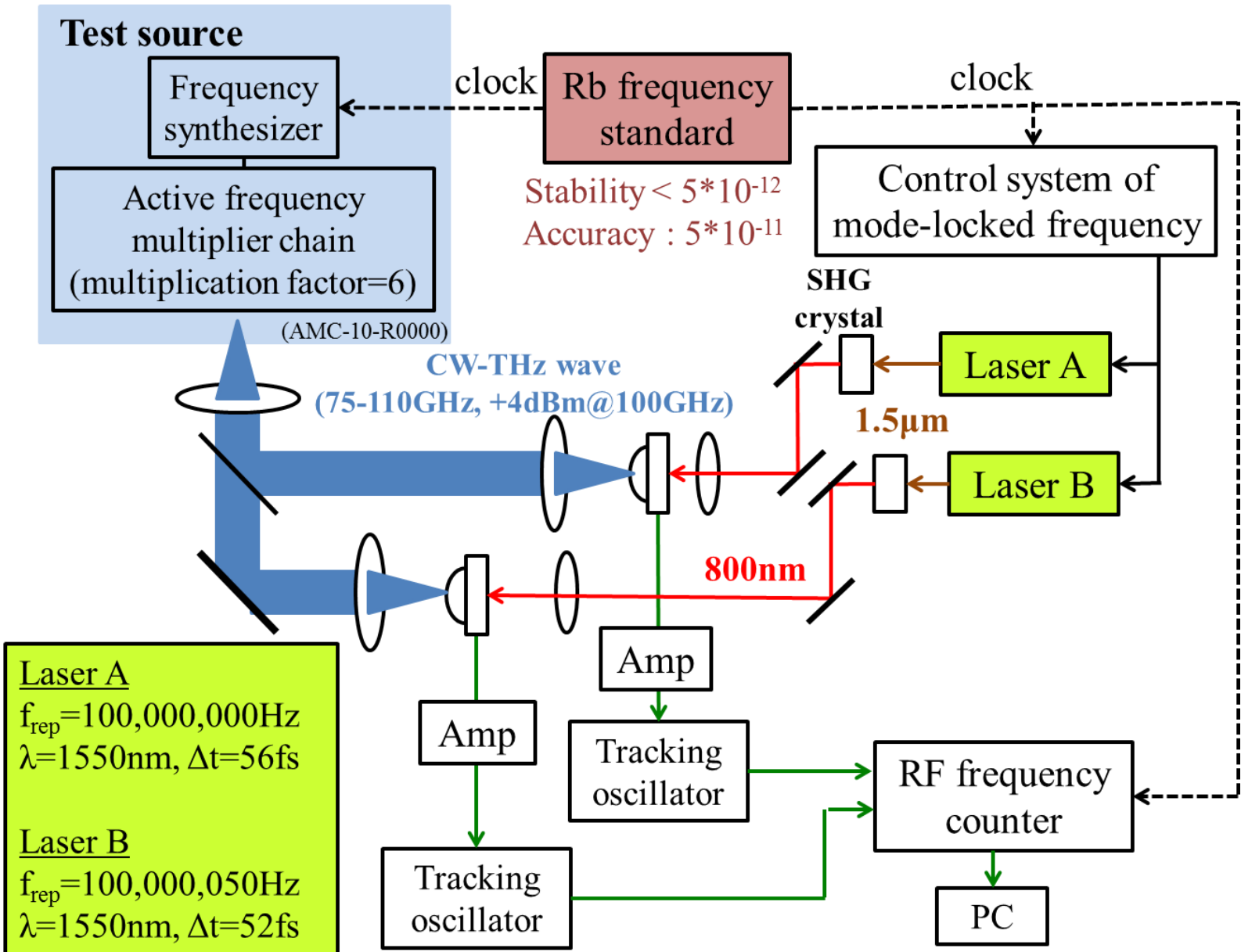


$$m = \frac{|f_{beat1} - f_{beat2}|}{|f_{rep1} - f_{rep2}|}$$

$$f_{THz} = mf_{rep1} - f_{beat1} \quad (\delta f_{beat} / \delta f_{rep} > 0)$$

$$f_{THz} = mf_{rep1} + f_{beat1} \quad (\delta f_{beat} / \delta f_{rep} < 0)$$

# Experimental setup

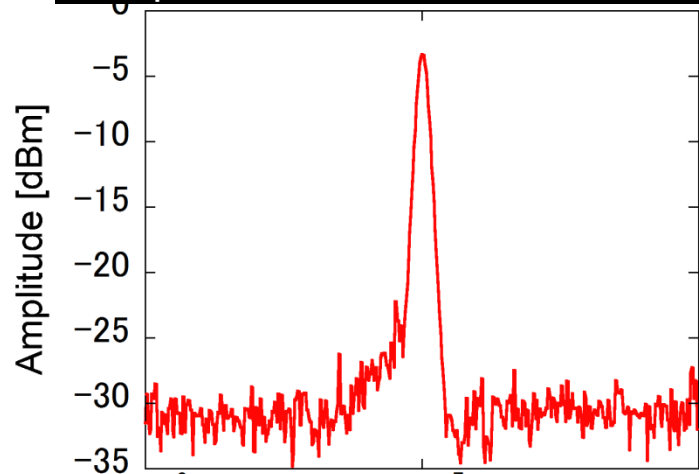




# Beat signals between CW-THz wave and dual PC-THz comb

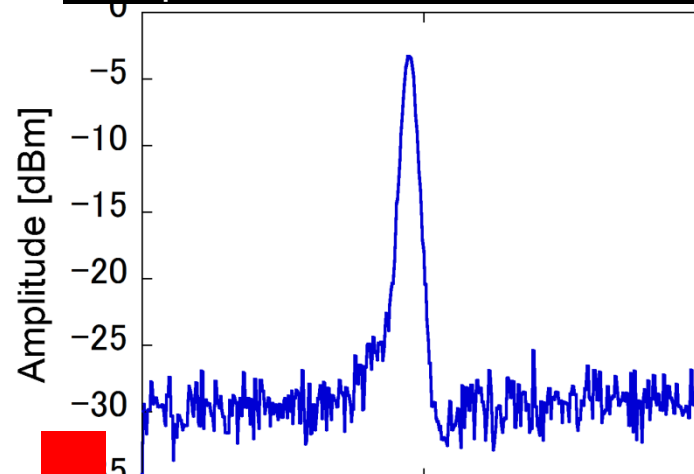
PC-THz comb (1)

( $f_{\text{rep1}} = 100,000,000$  Hz)



PC-THz comb (2)

( $f_{\text{rep2}} = 100,000,050$  Hz)



**Real-time determination!**

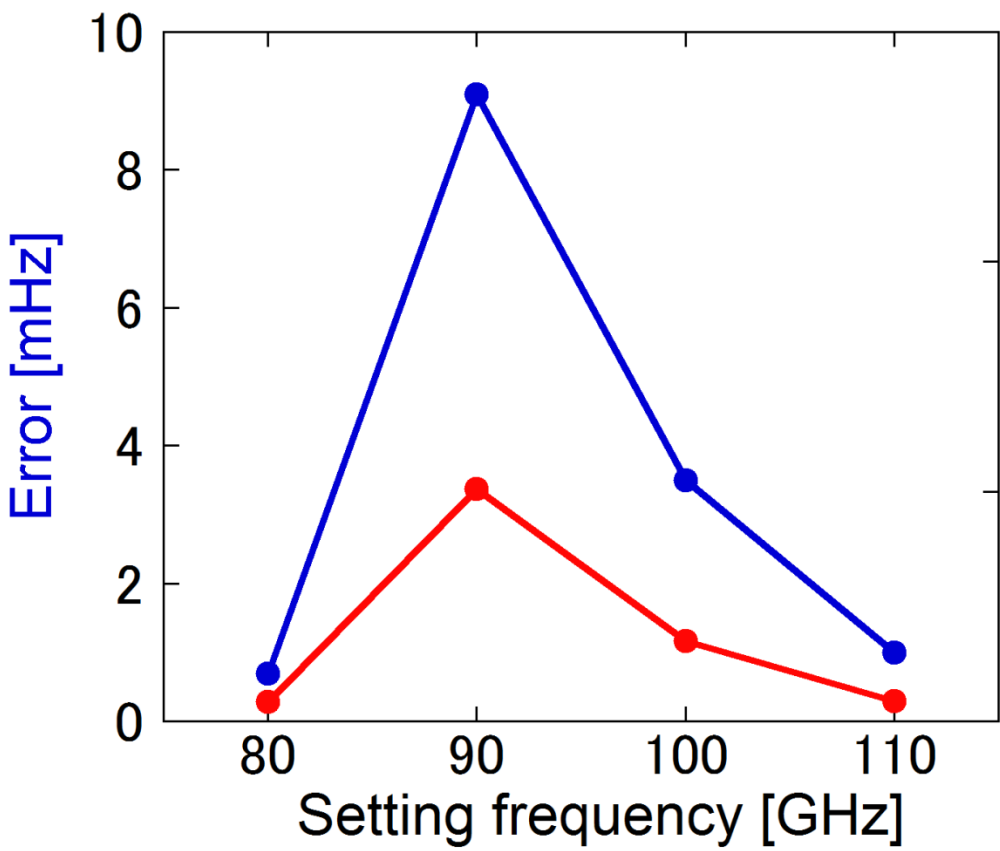
$$m = |f_{\text{beat1}} - f_{\text{beat2}}| / |f_{\text{rep1}} - f_{\text{rep2}}|$$

$$= |10,004,000.01 - 9,953,700.002| / |100,000,000 - 100,000,050| = 1006$$

$$f_{\text{THz}} = m f_{\text{rep1}} + f_{\text{beat1}} = 1006 * 100,000,000 + 10,004,000.01 = 100,610,004,000 \text{ Hz}$$



# Accuracy of absolute frequency measurement



30 [ $\times 10^{-14}$ ]

Estimation of measurement error

$$f_{THz} = mf_{rep1} + f_{beat1}$$

$$Df_{THz} = mDf_{rep1} + Df_{beat1}$$

Accuracy

$$\Delta f_{rep1} = 400\mu\text{Hz}$$

$$\Delta f_{beat1} = 21\text{mHz}$$

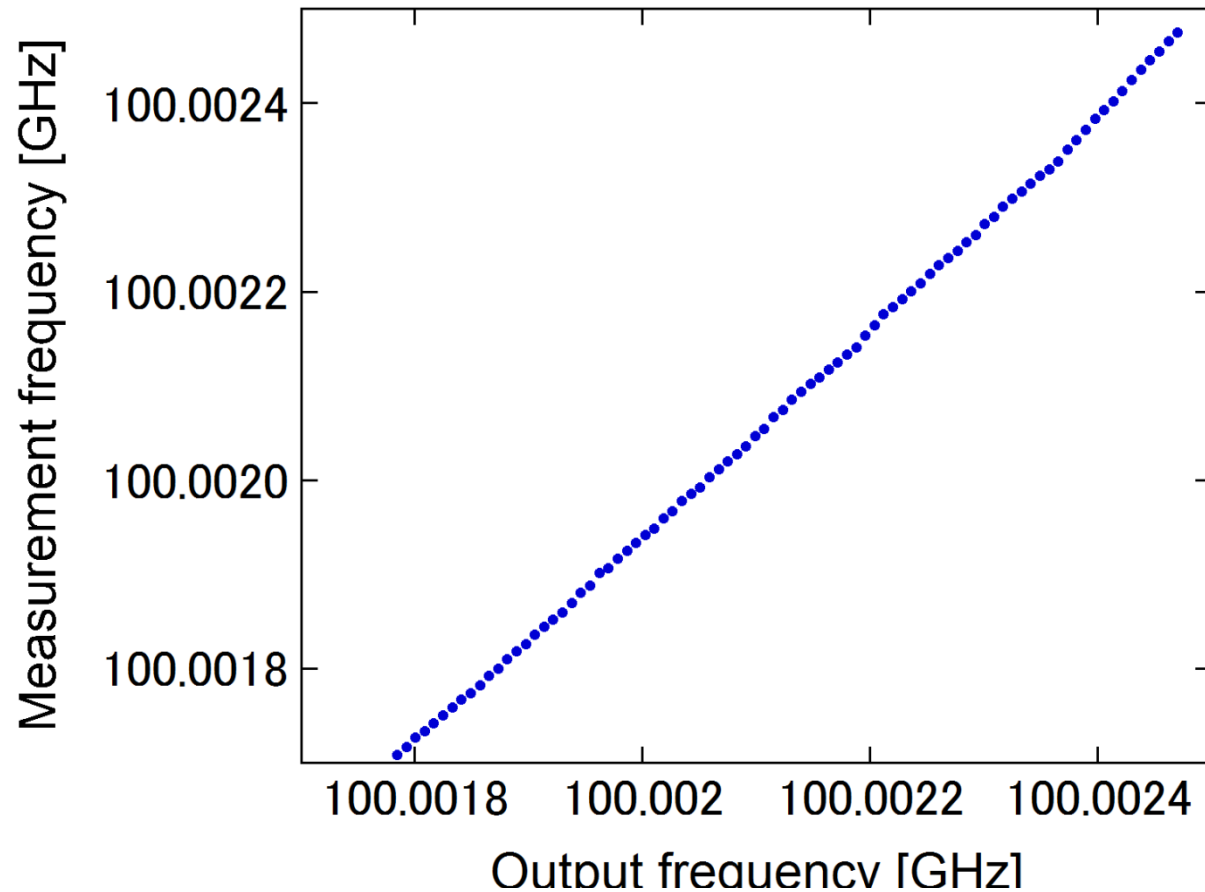
$$m = 800 \sim 1100$$

↓

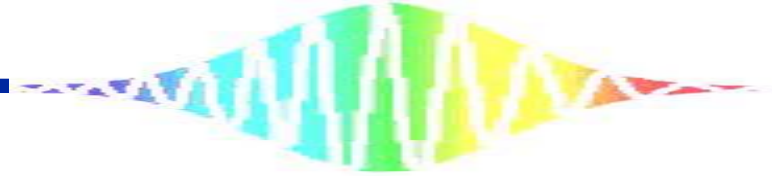
$$\Delta f_{THz} = 341 \sim 461\text{mHz}$$

Mean precision= $3.8 \times 10^{-14}$

# Real-time monitoring of linearly frequency-swept CW-THz wave



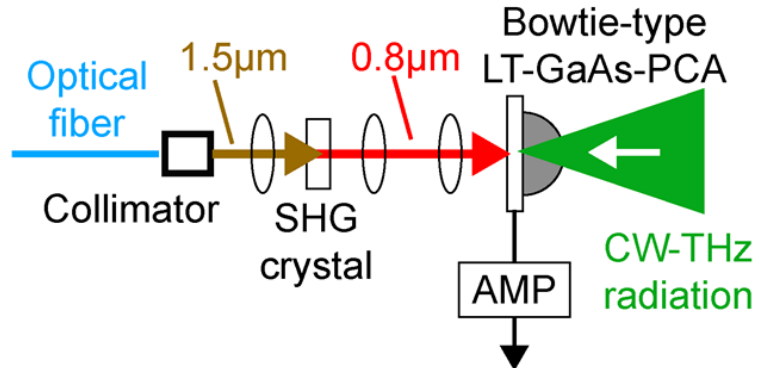
Linear sweep



(2) Direct coupling of LT-GaAs-PCA with output fiber tip of 1.5 $\mu\text{m}$  fiber laser

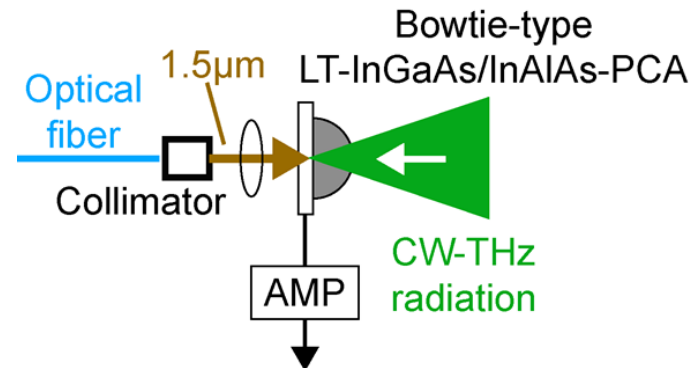
# Coupling methods of PCA with 1.5- $\mu\text{m}$ light

(1) SHG & lenses @ LT-GaAs PCA



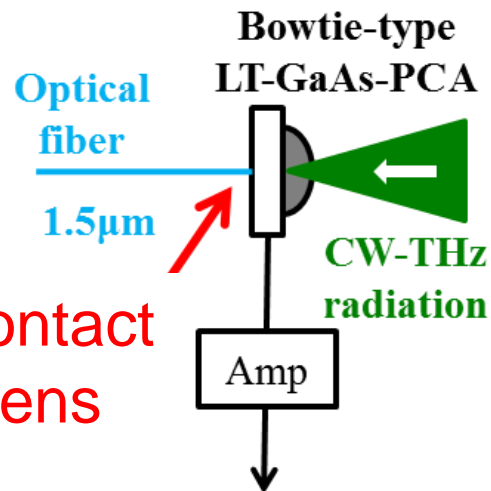
Several free-space optics required

(2) lenses @ LT-InGaAs PCA



Low sensitivity

(3) No optical components @ LT-GaAs PCA



Direct contact without lens

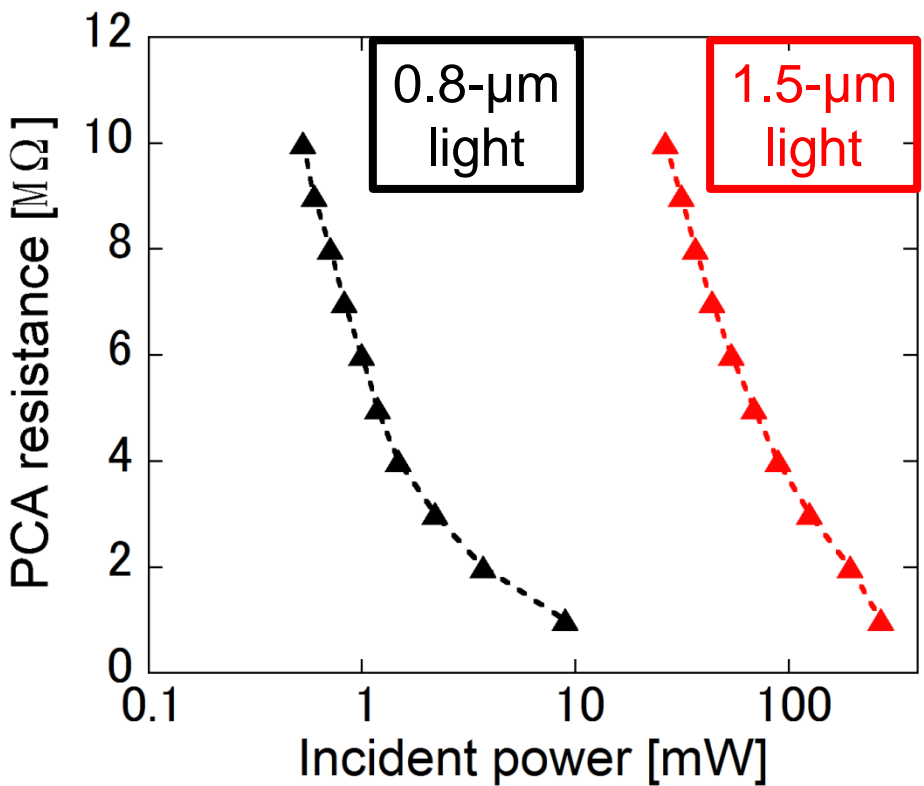
No free-space, no optics, and moderate sensitivity



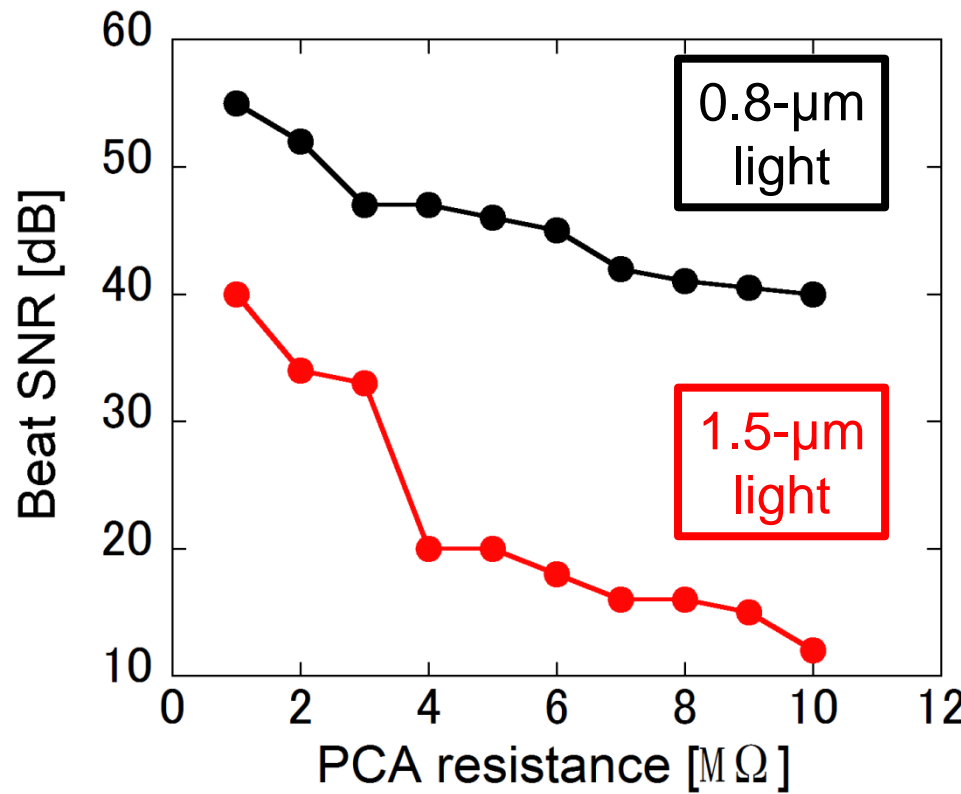
# Comparison between 0.8- $\mu\text{m}$ and 1.5- $\mu\text{m}$ lights

Beat frequency 100kHz (amp 100kHz, 50M $\Omega$ ), RBW=3kHz

Dependence of PCA resistance on incident power



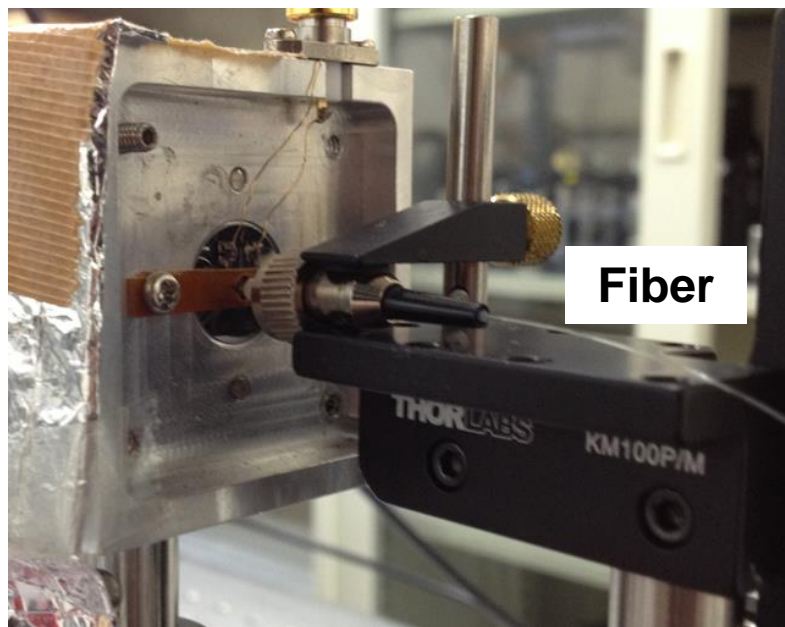
Dependence of beat SNR on PCA resistance



# Results

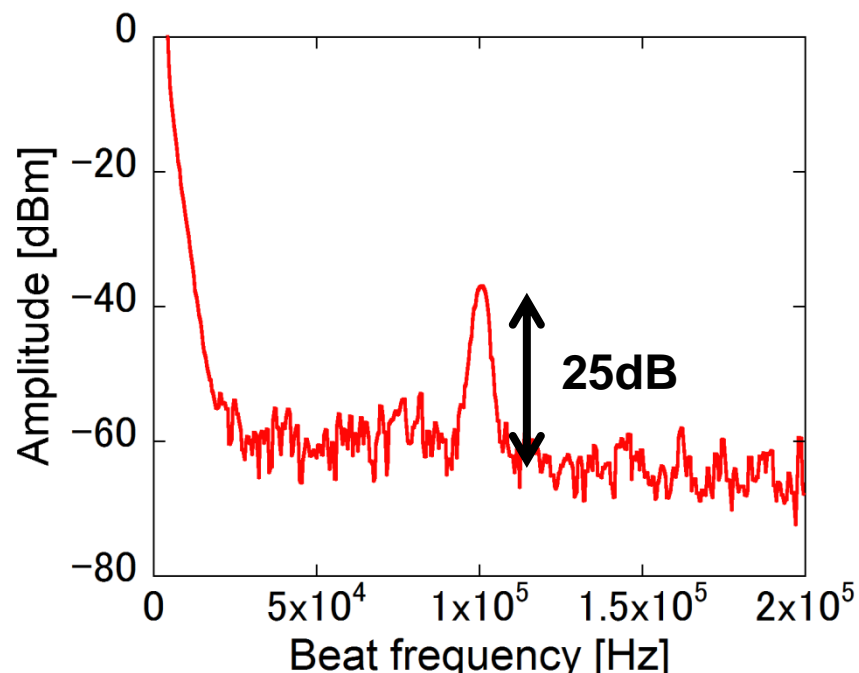
Direct fiber coupling without lens

( $P_{\text{mean}} = 189\text{mW}$ ,  $f_{\text{rep}} = 56\text{MHz}$ )

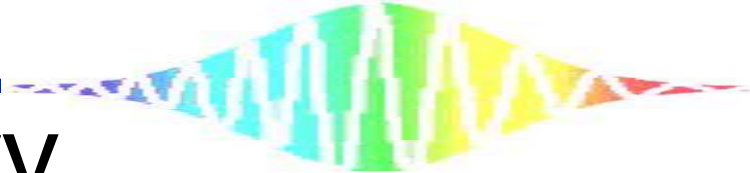


RF spectrum of  $f_b$  beat signal

( $f_{\text{beat}} = 100\text{kHz}$ )



Direct fiber coupling enables us to construct compact, robust, maintenance-free THz spectrum analyzer for portable use in practical applications!



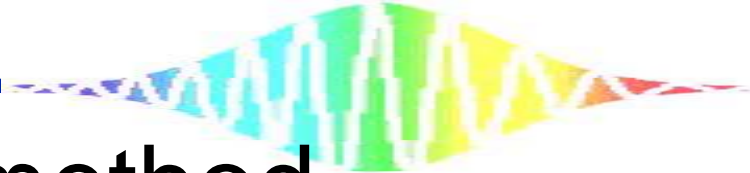
# Summary

- (1) Real-time determination of absolute frequency of CW-THz wave using dual PC-THz combs
- (2) Direct coupling of LT-GaAs-PCA with output fiber tip of 1.5 $\mu\text{m}$  fiber laser, enabling us to construct a portable system

## Future works

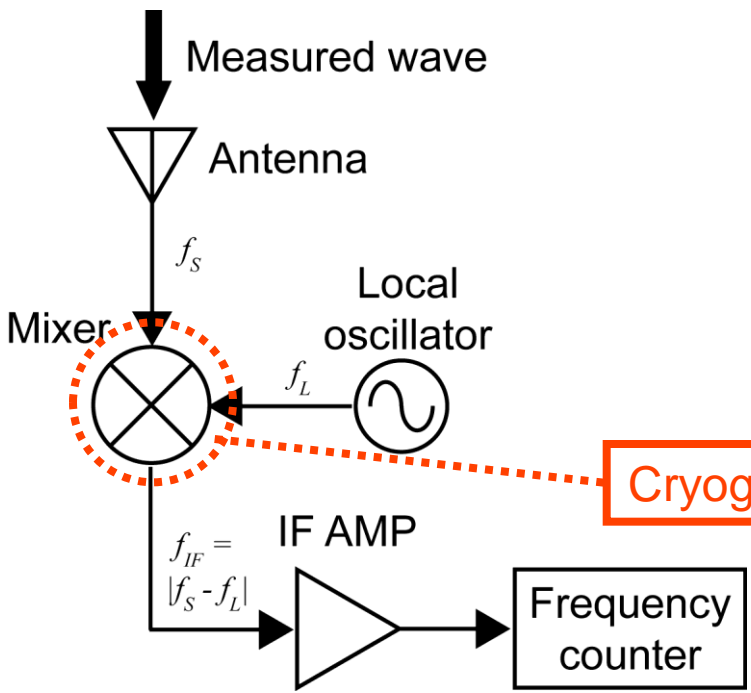
- (1) Real-time determination of absolute frequency using a single PC-THz comb
- (2) Integration of PCA, fiber tip, and amplifier



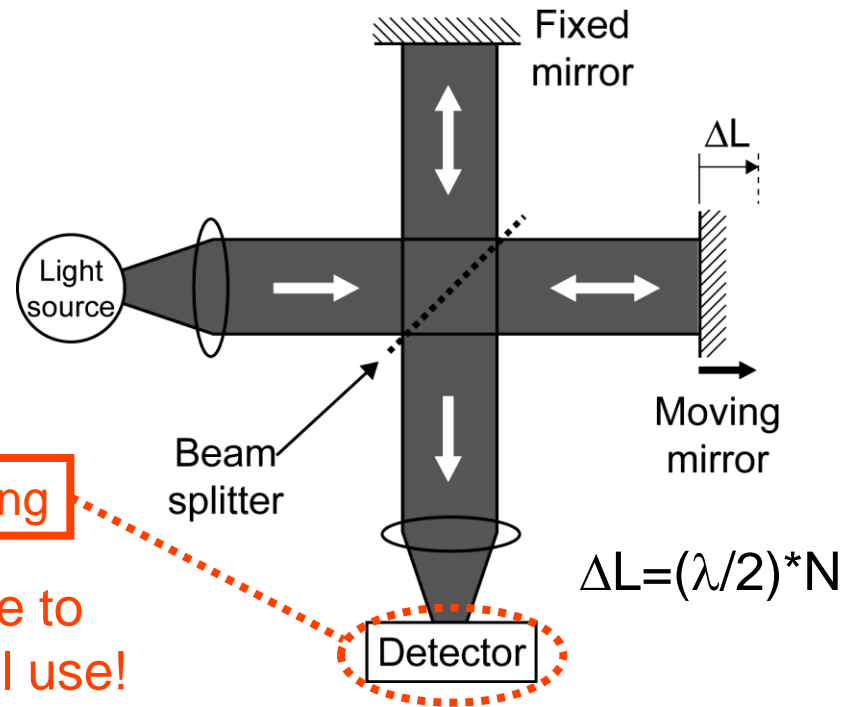


# Conventional method

## Electrical heterodyned method



## Optical interferometric method



Cryogenic cooling

Obstacle to practical use!

Difficult to cover all frequency region of THz wave (0.1~10THz)

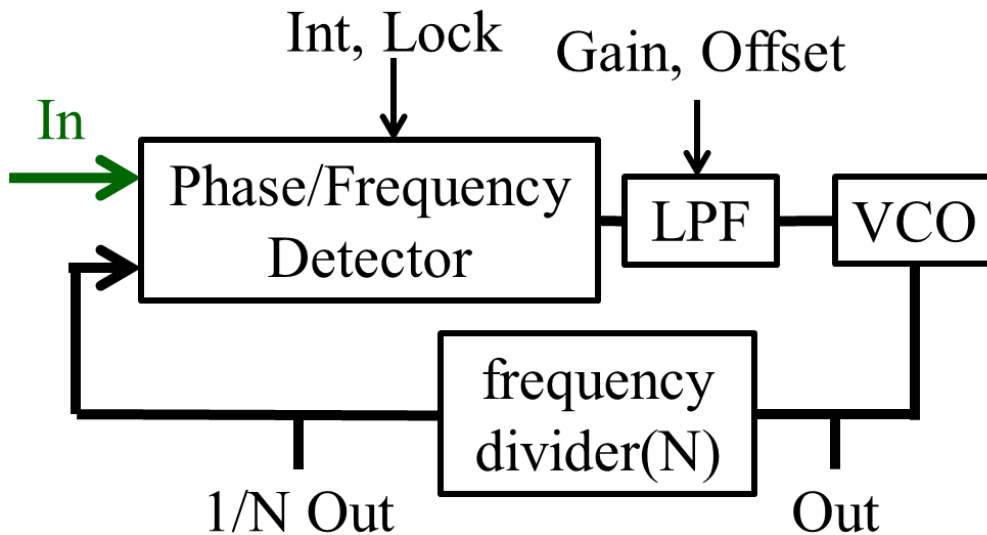
→ Requirement of new method optimized for THz wave!

# Tracking Oscillator

位相同期により入力信号を増幅

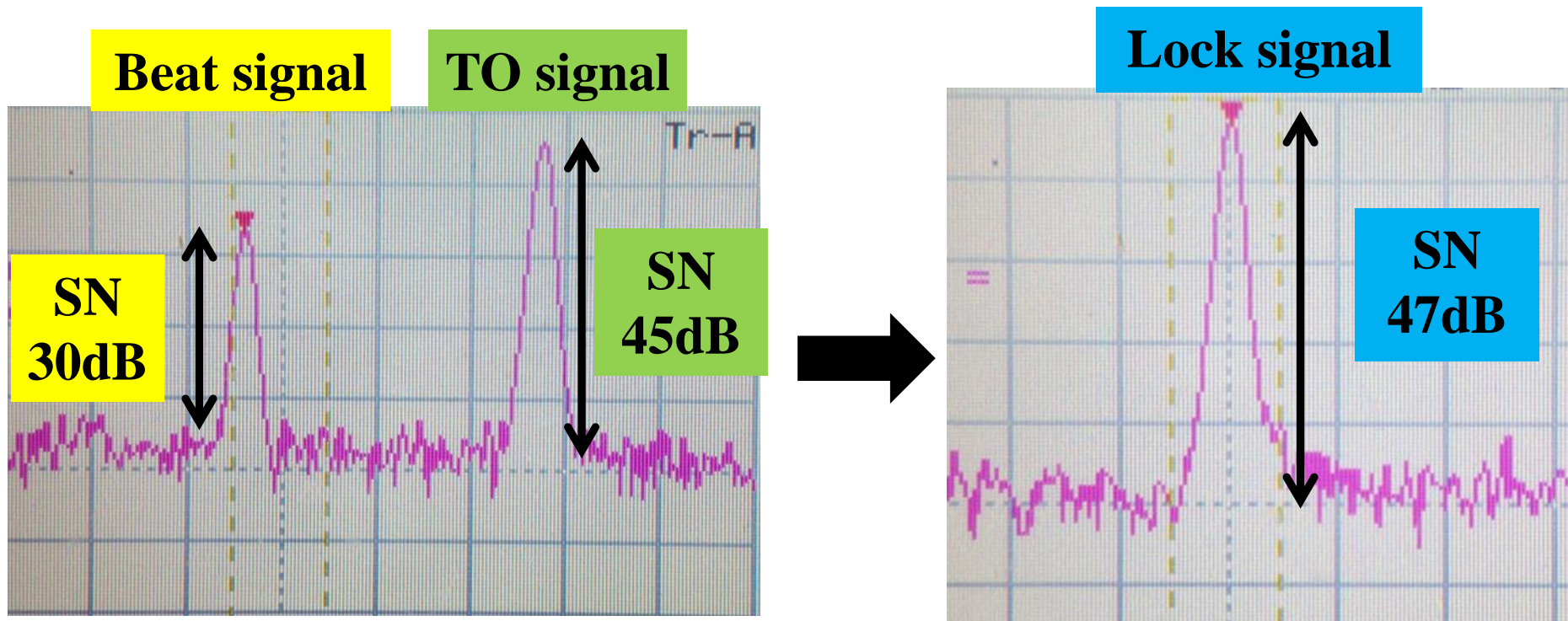
入力周波数の変動はVCOがトラッキングし、位相同期を維持

SN比の向上



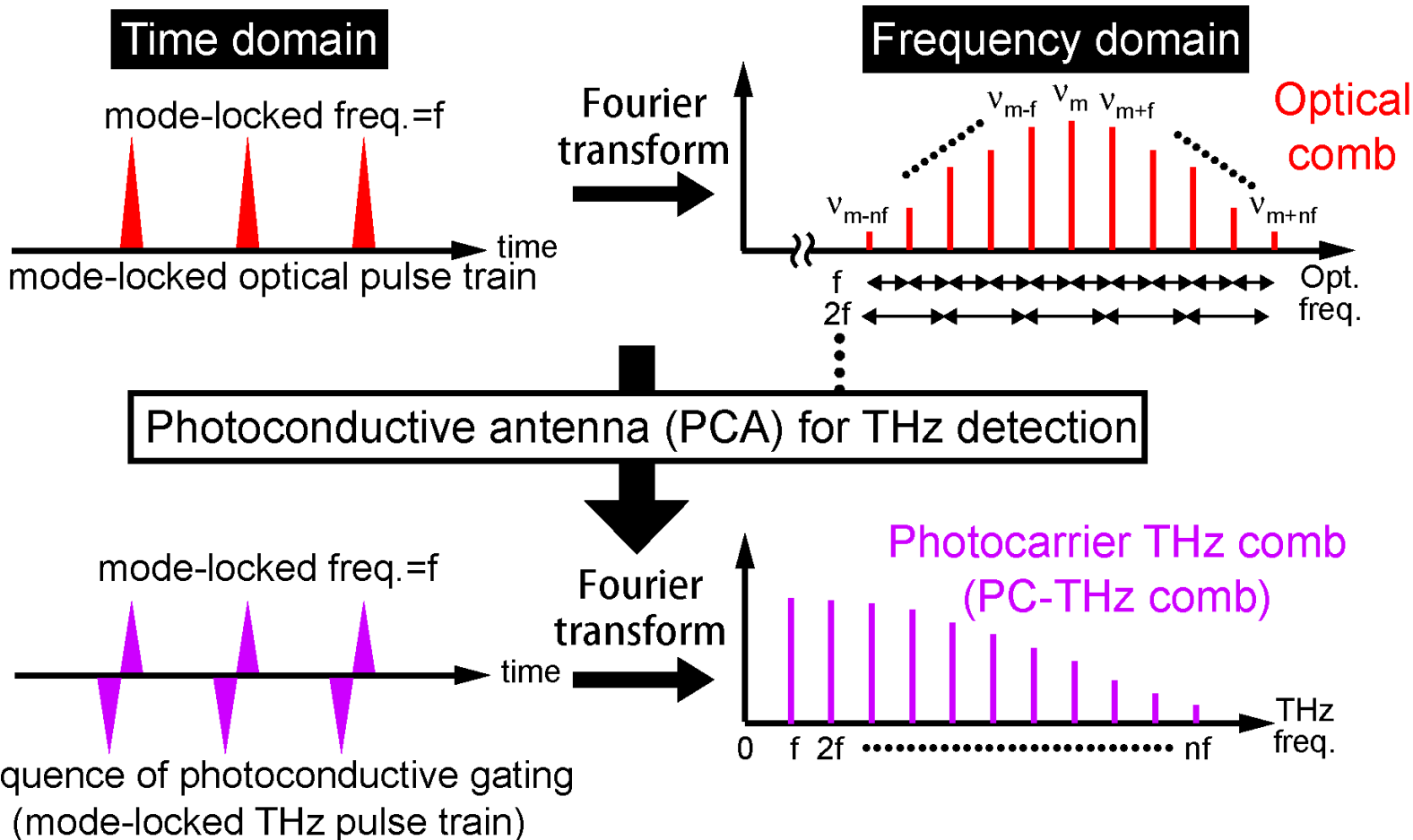
トラッキングオシレーターを用いて絶対周波数のリアルタイム測定を目指す

# Tracking Oscillator の特性評価



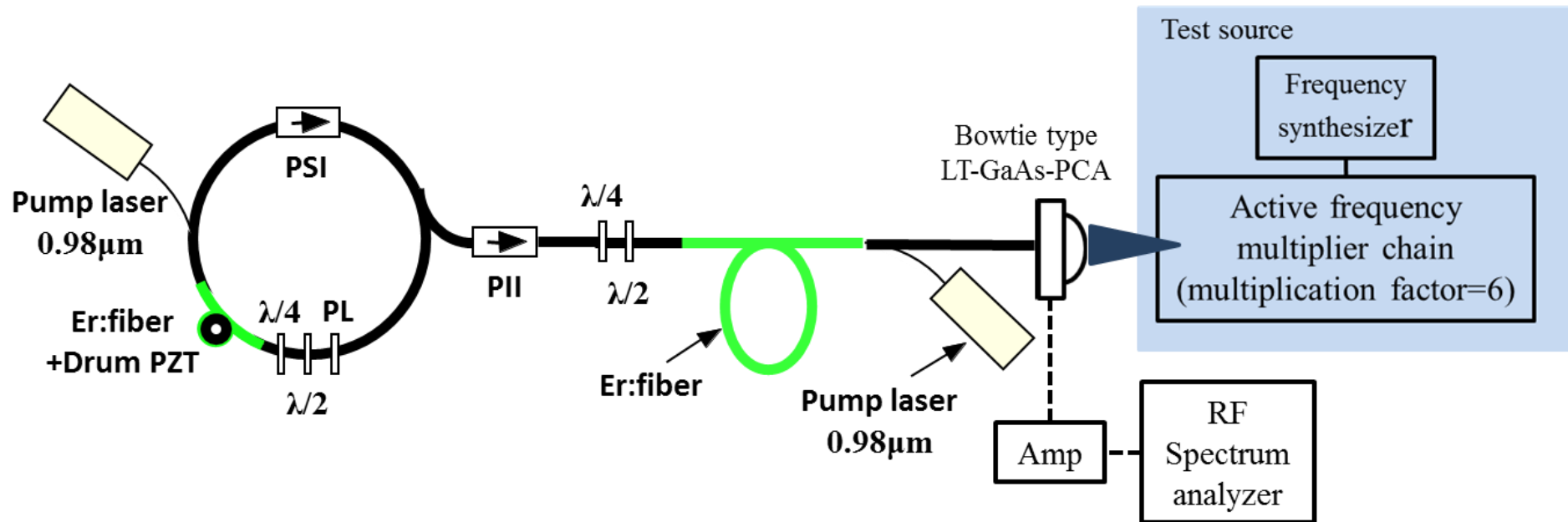
最低30dB (RBW10kHz) のビート信号において  
トラッキングオシレーターでロック可能

# Optical comb and THz comb



Simple, broadband selectivity, high spectral purity, offset free, and absolute frequency calibration

## ② Experimental setup



### Er:fiber laser

Center wavelength  $1550\text{nm}$

Repetition rate  $56\text{MHz}$

Pulse width  $47\text{fs}$

Average power  $189\text{mW}$